

Stat Review Handbook
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Psych 420

Data

Subjects	Aggression Difference Scores	Locus of Control	Video Type	Gender	Class Level	Age	Major
1	-10	18	Non-aggressive	Female	Junior	20	Psychology
2	-13	6	Non-aggressive	Female	Freshman	18	Biology
3	2	9	Non-aggressive	Female	Freshman	18	Biology
4	-3	8	Aggressive	Female	Sophomore	20	Art
5	16	17	Aggressive	Female	Freshman	19	Child Development
6	-9	8	Aggressive	Female	Senior	23	Psychology/Biology
7	0	10	Non-aggressive	Female	Junior	33	Health Administration
8	3	11	Non-aggressive	Male	Freshman	18	Business
9	2	11	Non-aggressive	Male	Sophomore	20	Journalism
10	-7	9	Aggressive	Female	Junior	20	Psychology
11	-6	11	Aggressive	Female	Sophomore	19	Psychology/Child Development
12	2	9	Aggressive	Male	Freshman	19	English Literature
13	3	16	Non-aggressive	Female	Junior	20	Physical Therapy
14	-21	6	Non-aggressive	Female	Freshman	18	Political Science
15	-4	10	Non-aggressive	Male	Senior	21	Computer Science
16	3	8	Non-aggressive	Female	Freshman	18	Accounting
17	-5	10	Non-aggressive	Female	Freshman	18	Undecided
18	-9	8	Non-aggressive	Male	Sophomore	19	Biology
19	-9	14	Aggressive	Male	Junior	20	Psychology
20	-6	11	Aggressive	Female	Sophomore	19	Health Science
21	3	10	Aggressive	Female	Freshman	19	Child Development
22	-10	6	Non-aggressive	Female	Senior	23	Biology
23	6	11	Non-aggressive	Male	Sophomore	19	Criminology
24	-13	14	Non-aggressive	Female	Sophomore	19	Physical Therapy
25	-5	9	Aggressive	Male	Sophomore	20	Undecided
26	-5	5	Aggressive	Female	Sophomore	21	Undecided
27	-1	14	Aggressive	Male	Junior	20	Psychology
28	-15	9	Aggressive	Female	Junior	23	Psychology
29	1	12	Aggressive	Female	Freshman	22	Biology
30	4	15	Aggressive	Female	Freshman	18.5	Undecided

Mean and Standard Deviation

Subjects	DV	DV ²
1	-10	100
2	-13	169
3	2	4
4	-3	9
5	16	256
6	-9	81
7	0	0
8	3	9
9	2	4
10	-7	49
11	-6	36
12	2	4
13	3	9
14	-21	441
15	-4	16
16	3	9
17	-5	25
18	-9	81
19	-9	81
20	-6	36
21	3	9
22	-10	100
23	6	36
24	-13	169
25	-5	25
26	-5	25
27	-1	1
28	-15	225
29	1	1
30	4	16
$\Sigma x = -106$		$\Sigma x^2 = 2026$

$$\bar{X} = \frac{\sum x}{N}$$

$$\text{Sample SD} = \sqrt{\frac{\sum x^2 - \frac{(\sum x)^2}{N}}{N}}$$

$$\text{Estimated Population SD} = \sqrt{\frac{\sum x^2 - \frac{(\sum x)^2}{N}}{N-1}}$$

$$N = 30$$

$$\sum x = -106$$

$$\sum x^2 = 2026$$

$$(\sum x)^2 = 11236$$

$$\bar{X} = \frac{-106}{30} = -3.5333$$

$$\text{sample } SD_N = \sqrt{\frac{2026 - \frac{(-106)^2}{30}}{30}} = \sqrt{\frac{2026 - \frac{11236}{30}}{30}} = \sqrt{\frac{2026 - 374.5333}{30}}$$

$$= \sqrt{\frac{1651.4667}{30}} = \sqrt{55.0489} = 7.4195$$

$$\text{estimated population } SD_{N-1} = \sqrt{\frac{2026 - \frac{(-106)^2}{30}}{30-1}} = \sqrt{\frac{2026 - \frac{11236}{30}}{29}}$$

$$= \sqrt{\frac{2026 - 374.5333}{29}} = \sqrt{\frac{1651.4667}{29}} = \sqrt{56.9471} = 7.5463$$

Z-scores

Subjects	DV	z-scores
1	-10	-0.86
2	-13	-1.25
3	2	0.73
4	-3	0.07
5	16	2.59
6	-9	-0.72
7	0	0.47
8	3	0.87
9	2	0.73
10	-7	-0.46
11	-6	-0.33
12	2	0.73
13	3	0.87
14	-21	-2.31
15	-4	-0.06
16	3	0.87
17	-5	-0.19
18	-9	-0.72
19	-9	-0.72
20	-6	-0.33
21	3	0.87
22	-10	-0.86
23	6	1.26
24	-13	-1.25
25	-5	-0.19
26	-5	-0.19
27	-1	0.34
28	-15	-1.52
29	1	0.60
30	4	1.00

$$z = \frac{x - \bar{x}}{SD}$$

$$z = \frac{-10 - (-3.5333)}{7.5463}$$

$$z = -.856936512$$

$$z = -.86$$

Transforming Scores to a Different Scale

Subjects	DV	z-scores
1	-10	-0.86
2	-13	-1.25
3	2	0.73
4	-3	0.07
5	16	2.59
6	-9	-0.72
7	0	0.47
8	3	0.87
9	2	0.73
10	-7	-0.46
11	-6	-0.33
12	2	0.73
13	3	0.87
14	-21	-2.31
15	-4	-0.06
16	3	0.87
17	-5	-0.19
18	-9	-0.72
19	-9	-0.72
20	-6	-0.33
21	3	0.87
22	-10	-0.86
23	6	1.26
24	-13	-1.25
25	-5	-0.19
26	-5	-0.19
27	-1	0.34
28	-15	-1.52
29	1	0.60
30	4	1.00

$$\text{New scale score} = SD(z) + \bar{x}$$

a. SAT

$$SD = 100, \bar{x} = 500$$

$$s = 100(-.87) + 500$$

$$s = -87 + 500 = 413$$

b. Stanford-Binet Intelligence Test

$$SD = 16, \bar{x} = 100$$

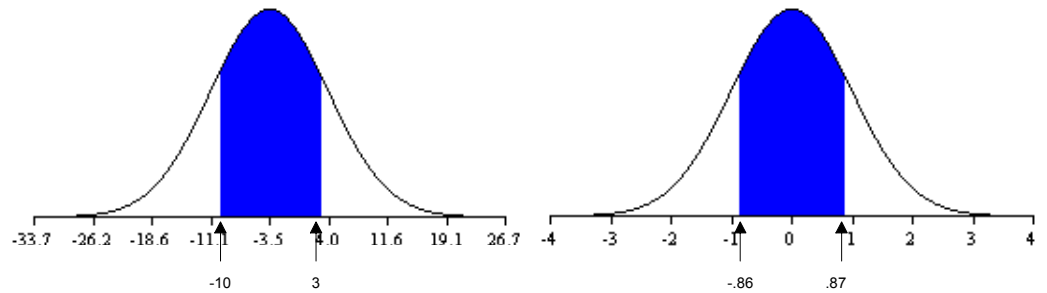
$$s = 16(-.87) + 100$$

$$s = -13.92 + 100 = 86.08 \approx 86$$

Area Under a Normal Curve
Assuming a normal curve

Subjects	DV	z-scores
1	-10	-0.86
2	-13	-1.25
3	2	0.73
4	-3	0.07
5	16	2.59
6	-9	-0.72
7	0	0.47
8	3	0.87
9	2	0.73
10	-7	-0.46
11	-6	-0.33
12	2	0.73
13	3	0.87
14	-21	-2.31
15	-4	-0.06
16	3	0.87
17	-5	-0.19
18	-9	-0.72
19	-9	-0.72
20	-6	-0.33
21	3	0.87
22	-10	-0.86
23	6	1.26
24	-13	-1.25
25	-5	-0.19
26	-5	-0.19
27	-1	0.34
28	-15	-1.52
29	1	0.60
30	4	1.00

a. The area between two scores on opposite sides of the distribution

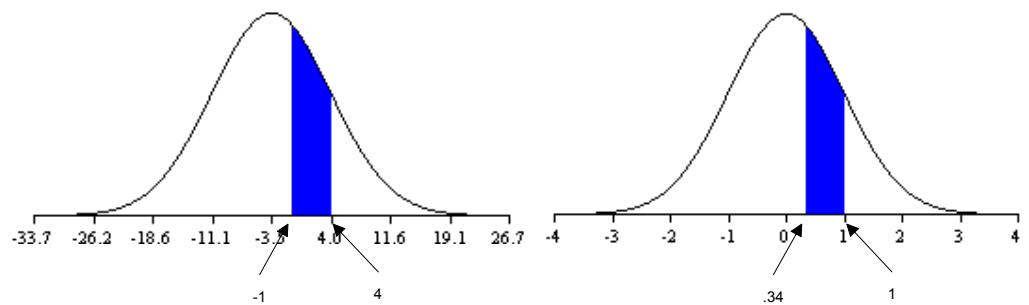


The area from the mean to -0.86 is the same as the area from the mean to $+0.86$. The area from the mean to $+0.86 = .3051$.

The area from the mean to $.87 = .3078$.

The two areas together equals $.3051 + .3078 = .6129$.

b. The area between two scores on the same side of the distribution.



The area from 0 to 1.00 = .3413.

The area from 0 to .34 = .1331.

The area from .34 to 1.00 = $.3413 - .1331 = .2082$.

Correlation Coefficient

Subjects	(X) LOC	(Y) DV	(X)(Y)	X ²	Y ²
1	18	-10	-180	324	100
2	6	-13	-78	36	169
3	9	2	18	81	4
4	8	-3	-24	64	9
5	17	16	272	289	256
6	8	-9	-72	64	81
7	10	0	0	100	0
8	11	3	33	121	9
9	11	2	22	121	4
10	9	-7	-63	81	49
11	11	-6	-66	121	36
12	9	2	18	81	4
13	16	3	48	256	9
14	6	-21	-126	36	441
15	10	-4	-40	100	16
16	8	3	24	64	9
17	10	-5	-50	100	25
18	8	-9	-72	64	81
19	14	-9	-126	196	81
20	11	-6	-66	121	36
21	10	3	30	100	9
22	6	-10	-60	36	100
23	11	6	66	121	36
24	14	-13	-182	196	169
25	9	-5	-45	81	25
26	5	-5	-25	25	25
27	14	-1	-14	196	1
28	9	-15	-135	81	225
29	12	1	12	144	1
30	15	4	60	225	16
SUM	315	-106	-821	3625	2026

Correlation between Change in aggression (DV) and Locus of control (LOC)

$$\sum X = 315, \sum Y = -106$$

$$\sum X^2 = 3625, \sum Y^2 = 2026$$

$$\sum XY = -821, N = 30,$$

$$(\sum X)^2 = 99225, (\sum Y)^2 = 11236$$

$$r = \frac{\sum XY - [(\sum X)(\sum Y)] / N}{\sqrt{\left[\sum X^2 - \frac{(\sum X)^2}{N}\right] \left[\sum Y^2 - \frac{(\sum Y)^2}{N}\right]}}$$

$$r = \frac{(-821) - [(315)(-106)] / 30}{\sqrt{\left[3625 - \frac{(315)^2}{30}\right] \left[2026 - \frac{(-106)^2}{30}\right]}}$$

$$r = \frac{(-821) - (-1113)}{\sqrt{[3625 - 3307.5][2026 - 374.53]}}$$

$$r = \frac{292}{\sqrt{(317.5)(1651.47)}}$$

$$r = \frac{292}{724.1144} = .4033$$

Linear Regression with a single predictor

Subjects	(X) LOC	(Y) DV	Z- scores (X)	Z- scores (Y)
1	18	-10	2.27	-0.86
2	6	-13	-1.36	-1.25
3	9	2	-0.45	0.73
4	8	-3	-0.76	0.07
5	17	16	1.96	2.59
6	8	-9	-0.76	-0.72
7	10	0	-0.15	0.47
8	11	3	0.15	0.87
9	11	2	0.15	0.73
10	9	-7	-0.45	-0.46
11	11	-6	0.15	-0.33
12	9	2	-0.45	0.73
13	16	3	1.66	0.87
14	6	-21	-1.36	-2.31
15	10	-4	-0.15	-0.06
16	8	3	-0.76	0.87
17	10	-5	-0.15	-0.19
18	8	-9	-0.76	-0.72
19	14	-9	1.06	-0.72
20	11	-6	0.15	-0.33
21	10	3	-0.15	0.87
22	6	-10	-1.36	-0.86
23	11	6	0.15	1.26
24	14	-13	1.06	-1.25
25	9	-5	-0.45	-0.19
26	5	-5	-1.66	-0.19
27	14	-1	1.06	0.34
28	9	-15	-0.45	-1.52
29	12	1	0.45	0.60
30	15	4	1.36	1.00

$$\bar{X} = -3.5333, \bar{Y} = 10.5$$

$$\sum X = 315, \sum Y = -106$$

$$\sum X^2 = 3625, \sum Y^2 = 2026$$

$$\sum XY = -821, N = 30,$$

$$(\sum X)^2 = 99225, (\sum Y)^2 = 11236$$

$$r_{xy} = .4033$$

a. Raw score formula

$$b = \frac{\sum XY - [(\sum X)(\sum Y)] / N}{\sum X^2 - \frac{(\sum X)^2}{N}}$$

$$b = \frac{(-821) - [(315)(-106)] / 30}{3625 - \frac{(315)^2}{30}}$$

$$b = \frac{(-821) - (-1113)}{3625 - 3307.5} = \frac{292}{317.5} = .9197$$

$$a = \bar{Y} - b\bar{X} = -3.5333 - (.9197)10.5 = -13.1902$$

$$Y' = bx + a = (.9197)18 + (-13.1902) = 3.3655$$

b. Z-score formula

$$rZ_{LOC} = Z_{Aggression}$$

$$.4033(2.27) = .9155$$

Hypothesis Test That a Population Mean is a Certain Value
One-Sample t-test

1. $h_0 : \mu_y = 0$

2. $h_1 : \mu_y \neq 0$

$$S_{\bar{Y}} = \frac{SD_{N-1}}{\sqrt{N}} = \frac{7.5463}{\sqrt{30}} = \frac{7.5463}{5.4772} = 1.3778$$

or

$$S_{\bar{Y}} = \frac{SD_N}{\sqrt{N-1}} = \frac{7.4195}{\sqrt{30-1}} = \frac{7.4195}{5.3852} = 1.3778$$

3. $t = \frac{\bar{Y} - \mu_Y}{S_{\bar{Y}}} = \frac{-3.5333}{1.3778} = -2.5645$

4. Reject h_0 if $|t| >$ critical value, otherwise do not reject h_0 .

Critical Value: $\alpha = .05$, $df = N - 1 = 30 - 1 = 29$;

Critical value from t-table = 2.04

Since $2.5645 > 2.04$, reject h_0 .

5. There is sufficient evidence that the population mean of aggression scores is non-zero.

T-Test for Correlation

$$r_{xy} = .4033$$

$$t_{correlation} = \frac{r\sqrt{n_{pairs} - 2}}{\sqrt{1 - r^2}}$$

1. $h_0 : \rho_{xy} = 0$

2. $h_1 : \rho_{xy} \neq 0$

$$t = \frac{.4033\sqrt{30 - 2}}{\sqrt{1 - .4033^2}} = \frac{.4033\sqrt{28}}{\sqrt{1 - .1627}}$$

3. $t = \frac{.4033(5.2915)}{\sqrt{.8373}} = \frac{2.1341}{.9150} = 2.3323$

4. Reject h_0 if $|t| >$ critical value, otherwise do not reject h_0 . The critical value with $\alpha = .05$, $df = 28$, two-tailed is 2.05. Since $2.3323 > 2.05$, reject h_0 .

5. There is sufficient evidence that the correlation between aggression scores and locus of control is greater than zero.

Two Independent Samples T-Test

(A) Aggressive	(B) Non- Aggressive
-3	-10
16	-13
-9	2
-7	0
-6	3
2	2
-9	3
-6	-21
3	-4
-5	3
-5	-5
-1	-9
-15	-10
1	6
4	-13

$$\bar{X}_A = -2.6667, SD_A = 7.3062$$

$$\bar{X}_B = -4.4, SD_B = 7.9355$$

$$t = \frac{\bar{X}_A - \bar{X}_B}{s_{\bar{X}_A - \bar{X}_B}}$$

$$s_{pooled}^2 = \frac{(n_A - 1)SD_A^2 + (n_B - 1)SD_B^2}{n_A + n_B - 2}$$

$$s_{\bar{X}_A - \bar{X}_B} = \sqrt{\frac{s_{pooled}^2}{n_A} + \frac{s_{pooled}^2}{n_B}}$$

1. $h_0 : \mu_A \leq \mu_B$

2. $h_0 : \mu_A > \mu_B$

$$s_{pooled}^2 = \frac{(15-1)7.3062^2 + (15-1)7.9355^2}{30-2} = \frac{747.32 + 881.61}{28} = 58.18$$

$$s_{\bar{X}_1 - \bar{X}_2} = \sqrt{\frac{58.18}{15} + \frac{58.18}{15}} = 2.78$$

3. $t = \frac{-2.6667 - (-4.4)}{2.78} = \frac{1.7333}{2.78} = .6234$

4. Reject h_0 if $|t| >$ critical value, otherwise do not reject h_0 . Critical value: $\alpha=.05$, $df=28$, one-tailed test. Tabled critical value is 1.70. Since 1.72 is larger than 1.7, reject h_0 .
5. There is evidence that there is a difference between the aggressive and non-aggressive groups.

Dependent Samples T-test (matched pairs t-test)

Subjects	Aggression Difference Scores	Locus of Control	Video Type	Gender
1	-10	18	Non-aggressive	Female
2	-13	6	Non-aggressive	Female
3	2	9	Non-aggressive	Female
4	-3	8	Aggressive	Female
5	16	17	Aggressive	Female
6	-9	8	Aggressive	Female
7	0	10	Non-aggressive	Female
8	3	11	Non-aggressive	Male
9	2	11	Non-aggressive	Male
10	-7	9	Aggressive	Female
11	-6	11	Aggressive	Female
12	2	9	Aggressive	Male
13	3	16	Non-aggressive	Female
14	-21	8	Non-aggressive	Female
15	-4	10	Non-aggressive	Male
16	3	8	Non-aggressive	Female
17	-5	10	Non-aggressive	Female
18	-9	8	Non-aggressive	Male
19	-9	14	Aggressive	Male
20	-6	11	Aggressive	Female
21	3	10	Aggressive	Female
22	-10	6	Non-aggressive	Female
23	6	11	Non-aggressive	Male
24	-13	14	Non-aggressive	Female
25	-5	9	Aggressive	Male
26	-5	5	Aggressive	Female
27	-1	14	Aggressive	Male
28	-15	9	Aggressive	Female
29	1	12	Aggressive	Female
30	4	15	Aggressive	Female

Subjects were matched on gender (each pair is designated by matching color)

Dependent Samples t-test (continued)

Pair	(A) Aggressive	(B) Non-Aggressive	A-B
1	16	-10	26
2	-3	-13	10
3	-9	2	-11
4	-7	0	-7
5	2	3	-1
6	-5	2	-7
7	-6	-21	15
8	-6	3	-9
9	3	-5	8
10	-5	-10	5
11	4	-13	17

$$\bar{X}_d = 4.1818, SD_d = 12.1967$$

$$t = \frac{\bar{X}_d - 0}{s_{\bar{d}}}$$

1. $h_0 : \mu_A \leq \mu_B$

2. $h_0 : \mu_A > \mu_B$

$$s_{\bar{d}} = \frac{SD_d}{\sqrt{n}} = \frac{12.1967}{\sqrt{11}} = 3.91$$

3. $t = \frac{4.1818 - 0}{3.91} = 1.07$

4. Reject h_0 if $|t| >$ critical value otherwise do not reject h_0 . Critical value: $\alpha = .05$, $df = 10$, two-tailed, tabled value = 2.23. Since, $1.07 < 2.23$ do not reject h_0 .

5. There is not enough evidence that there is a difference between the two groups.

“Goodness of Fit” test

Locus of Control Observed	
Internal	External
23	7

Locus of Control Expected	
Internal	External
15	15

$$\chi^2 = \sum \frac{(o - e)^2}{e}$$

$$\chi^2 = \sum \frac{(o - e)^2}{e} = \frac{(7 - 15)^2}{15} + \frac{(23 - 15)^2}{15} = \frac{64}{15} + \frac{64}{15} = 4.2667 + 4.2667 = 8.5334$$

1. $h_0 : P_{external} = .5$
2. $h_0 : P_{external} \neq .5$
3. $\chi^2 = \sum \frac{(o - e)^2}{e} = \frac{(7 - 15)^2}{15} + \frac{(23 - 15)^2}{15} = \frac{64}{15} + \frac{64}{15} = 4.2667 + 4.2667 = 8.5334$
4. Reject h_0 if $\chi^2 >$ critical value, otherwise do not reject h_0 . Critical value: $\alpha = .05$, $df = 1$, tabled value = 3.84. Since, $8.5334 > 3.84$ reject h_0 .
5. There is sufficient evidence that the probability of external LOC is not .5 or that the frequencies of internal and external locus of control are not equal.

Multiway contingency tables

	LOC		
	Internal	External	
Non-Aggressive	12	3	15
Aggressive	11	4	15
	23	7	

$$\chi^2 = \sum \frac{(o-e)^2}{e}$$

$$e = \frac{R * C}{T}$$

	LOC			LOC	
	Internal	External		Internal	External
Non-Aggressive	$\frac{(23)(15)}{30}$	$\frac{(7)(15)}{30}$	→	11.5	11.5
Aggressive	$\frac{(23)(15)}{30}$	$\frac{(7)(15)}{30}$	→	3.5	3.5

1. h0: Video type and LOC are independent
2. h1: Video type and LOC are independent

$$3. \chi^2 = \sum \frac{(o-e)^2}{e} = \frac{(12-11.5)^2}{11.5} + \frac{(11-11.5)^2}{11.5} + \frac{(3-3.5)^2}{3.5} + \frac{(4-3.5)^2}{3.5} = .0217 + .0217 + .0714 + .0714 = .1862$$

4. Reject h0 if $\chi^2 >$ critical value, otherwise do not reject h0. Critical value: $\alpha = .05$, $df = (\#column - 1)(\#rows - 1) = 1$, tabled value = 3.84. Since, $.1862 < 3.84$ do not reject h0.
5. There is insufficient evidence that LOC and video type are related (dependent).